

SWOT INSTITUTE

RELATIONS AND FUNCTIONS

XI-TEST

Time : 1 hr.

1. If $\left(\frac{x}{3} + 1, y - \frac{2}{3}\right) = \left(\frac{5}{3}, \frac{1}{3}\right)$, find the value of x and y .
2. If $A = \{-1, 1\}$, find $A \times A \times A$.
3. Let $A = \{1, 2\}$ and $B = \{3, 4\}$. Write $A \times B$. How many subsets will $A \times B$ have ? List them.
4. Let $A = \{1, 2, 3, \dots, 14\}$. Define a relation R from A to A by $R = \{(x, y) : 3x - y = 0, \text{ where } x, y \in A\}$. Write down its domain, codomain and range.
5. Determine the domain and range of the relation R defined by $R = \{(x, x + 5) : x \in \{0, 1, 2, 3, 4, 5\}\}$.
6. Find the domain and range of the following real functions :
 $f(x) = \sqrt{9 - x^2}$
7. The function 't' which maps temperature in degree Celcius into temperature in degree Fahreheit is defined by $n(C) = \frac{9C}{5} + 32$. Find :
(i) $t(0)$ (ii) $t(28)$ (iii) $t(-10)$ (iv) The value of C , when $t(C) = 212$.
8. Find the domain of the function $f(x) = \frac{x^2 + 3x + 5}{x^2 - 5x + 4}$.
9. If $f(x) = x^2$, find $\frac{f(1.1) - f(1)}{(1.1 - 1)}$
10. Find the domain of the function $f(x) = \frac{x^2 + 2x + 1}{x^2 - 8x + 12}$.
11. Let $f = \left\{ \left(x, \frac{x^2}{1+x^2} \right) : x \in \mathbb{R} \right\}$ be a function from \mathbb{R} into \mathbb{R} . Determine the range of f .
12. Let $f, g : \mathbb{R} \rightarrow \mathbb{R}$ be defined, respectively by $f(x) = x + 1$, $g(x) = 2x - 3$. Find $f + g$, $f - g$ and $\frac{f}{g}$.